

1-4 Videos Guide

1-4a

- Calculus of the natural logarithmic function
 - $\frac{d}{dx} [\ln|x|] = \frac{1}{x}, \quad x \neq 0$
 - $\int \frac{1}{x} dx = \ln|x| + C$

Exercise:

- Show that $\int \tan x dx = \ln|\sec x| + C$.

1-4b

Exercises:

- Differentiate the function
 - $f(x) = \ln(\sin^2 x)$
 - $h(x) = \ln(x + \sqrt{x^2 - 1})$
 - $y = \ln(\csc x - \cot x)$

1-4c

Exercises:

- Evaluate the integral.
 - $\int_0^3 \frac{dx}{5x+1}$
 - $\int \frac{\cos x}{2+\sin x} dx$

1-4d

- Calculus of logs and exponentials with bases other than e
 - $\frac{d}{dx} (\log_b x) = \frac{1}{x \ln b}$
 - $\frac{d}{dx} (b^x) = \ln b \cdot b^x$
 - $\int b^x dx = \frac{b^x}{\ln b} + C$

1-4e

Definition: (Euler's number e)

- $e = \lim_{x \rightarrow 0} (1 + x)^{1/x}$
- $e = \lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^n$

1-4f

Exercise:

- Use logarithmic differentiation to find the derivative of the function.

$$y = \frac{e^{-x} \cos^2 x}{x^2 + x + 1}$$

1-4g

Exercise:

- Use logarithmic differentiation to find the derivative of the function.
 $y = x^{\cos x}$
- Process for logarithmic differentiation
 - Take the natural log of both sides
 - Use properties of logs
 - Differentiate (usually with respect to x)—use implicit differentiation for y
 - Give $\frac{dy}{dx}$ or y' in terms of x (or whatever the independent variable is)
- Summary of techniques involving exponents
 - (variable base)^{constant exponent} —power rule (ex: $y = x^2$)
 - (constant base)^{variable exponent} —rules for exponentials (ex: $y = e^x$ or $y = 2^x$)
 - (variable base)^{variable exponent} —logarithmic differentiation